

Analysis of Effects of using 9/7 Wavelet Coefficients in Multi-resolution Analysis

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Abstract—Conventional distributed arithmetic (DA) is popular in field programmable gate array (FPGA) design, and it features on-chip ROM to achieve high speed and regularity. In this paper, we describe high speed area efficient 1-D discrete wavelet transform (DWT) using 9/7 filter based new efficient distributed arithmetic (NEDA) Technique. Being area efficient architecture free of ROM, multiplication, and subtraction, NEDA can also expose the redundancy existing in the adder array consisting of entries of 0 and 1. This architecture supports any size of image pixel value and any level of decomposition. The parallel structure has 100% hardware utilization efficiency.

Keywords: - 1-D Discrete Wavelet Transform (DWT), NEDA, Low Pass Filter, High Pass Filter, Xilinx Simulation.

I. INTRODUCTION

Discrete wavelet transform (DWT) is a mathematical technique that provides a new method for signal processing and decomposes a discrete signal in the time domain by using dilated / contracted and translated versions of a single basis function, named as prototype wavelet [Mallat (1989a) ; Mallat (1989b) ; Daubachies (1992) ; Meyer (1993) ; Vetterli and Kovacevic (1995)]. DWT offers wide variety of useful features over other unitary transforms like discrete Fourier transforms (DFT), discrete cosine transform (DCT) and discrete sine transform (DST). Some of these features are; adaptive time-frequency windows, lower aliasing distortion for signal processing applications, efficient computational complexity and inherent scalability [Grzesczak et al. (1996)]. Due to these features one dimensional (1-D) DWT and two dimensional (2-D) DWT are applied in various application such as numerical analysis [Beylkin et al. (1992)], signal analysis [Akanshu and Haddad (1992)], image coding [Sodagar et al. (1999); Taubman (2000)], pattern recognition [Kronland et al. (1987)], statistics [Stoksik et al. (1994)] and biomedicine [Senhadji et al. (1994)]. Several algorithms and computation schemes have been suggested during last three decades for efficient hardware implementation of 1-D DWT and 2-D DWT.

The DWT is computationally intensive and most of its application demand real-time processing. One way of achieving high speed performance is to use fast computational

Algorithm in a general purpose computers. Another way is to exploit the parallelism inherent in the computation for concurrent processing by a set of parallel processor. But, it is not cost effective to use a general purpose computer for a specific application. Also, general purpose computer used for their implementation required more space, large power and more computation time. With the development of very large scale integration (VLSI) technology it facilitates to digital signal processing (DSP) system designer to design a high performance, low cost and low power system in a single chip. The characteristic of VLSI system are that they offer greater potential for large amount of concurrency and offer an enormous amount of computing power within a small area [Weste and Eshraghian (1993)]. The computation is very cheap as the hardware is not an obstacle for VLSI system. But, the non-localized global communication is not only expensive but demands high power dissipation. Thus, a high degree of parallelism and a nearest neighbor communication are crucial for realization of high performance VLSI system [Kung (1982)]. Keeping this in view, high performance application specific VLSI systems are rapidly evolving in recent years. The special purpose VLSI systems maximize processing concurrency by parallel / pipeline processing and provides cost effective alternative for real-time application. Therefore, 2-D DWT is currently implemented in a VLSI system to meet the temporal requirement of real-time application. Keeping this fact in view, several design schemes have been suggested in the last two decades for efficient implementation of 2-D DWT in a VLSI system. Researchers have adopted different algorithm formulation, mapping scheme,

and architectural design methods to reduce the computational time, arithmetic complexity or memory complexity of 2-D DWT structures. However, the area-delay performance of the existing structures changes marginally. This is mainly due to the memory complexity, which forms a major hardware component of folded 2-D DWT structure. A detail study of the existing design methods and a complexity analysis is made in Chapter 2 to find an appropriate design strategy to improve the area-delay performance of 2-D DWT structures.

II. MULTILEVEL DISCRETE WAVELET TRANSFORM

Multiresolution analysis (MRA) is a characteristic feature of SB and it is used for better spectral representation of the signal. In MRA, the signal is decomposed for more than one DWT level known as multilevel DWT. It means the low-pass output of first DWT level is further decomposed in a similar manner in order to get the second level of DWT decomposition and the process is repeated for higher DWT levels. Few algorithms have been suggested for computation of multilevel DWT. One of the most important algorithm are pyramid algorithm (PA), this algorithm are proposed Mallet (1989a) for parallel computation of multilevel DWT. PA for 1-D DWT is given by

$$Y_l^j(n) = \sum_{i=0}^{k-1} h(i)Y_l^{j-1}(2n-i)$$

(1)

$$Y_h^j(n) = \sum_{i=0}^{k-1} g(i)Y_h^{j-1}(2n-i)$$

(2)

Where $Y_l^j(n)$ is the n-th low-pass sub band component of the j-th DWT level and $Y_h^j(n)$ is the n-th high-pass sub band component of the j-th DWT level. Two-dimensional signal, such as images, are analyzed using the 2-D DWT. Currently 2-D DWT is applied in many image processing applications such as image compression and reconstruction [Lewis and Knowles (1992)], pattern recognition [Kronland *et al.* (1987)], biomedicine [Senhadji *et al.* (1994)] and computer graphics [Meyer (1993)]. The 2-D DWT is a mathematical technique that decomposes an input image in the multiresolution frequency space. The 2-D DWT decomposes an input image into four sub bands known as low-low (LL), low-high (LH), high-low (HL) and high-high (HH) sub band.

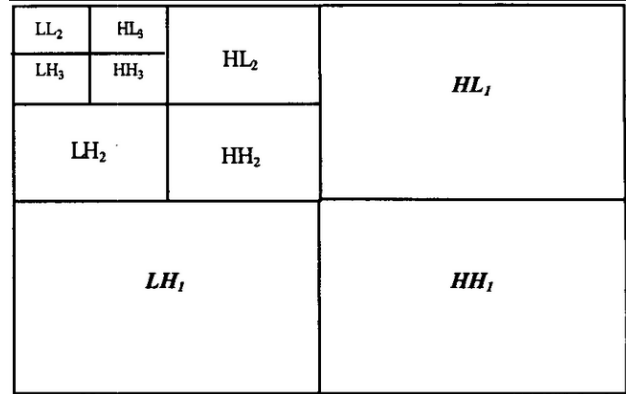


Figure 1: Figure 1: Three Level Diagram of 2-D Sub-band Wavelet Transform

III. PROPOSED ARCHITECTURE

The block diagram of 9/7 wavelet coefficient based multilevel discrete wavelet transform using NEDA structure shown in figure 2. In this figure, input sample passing through 8-bit register after that all symmetrical delay input is add in the equation 3 to equation 7.

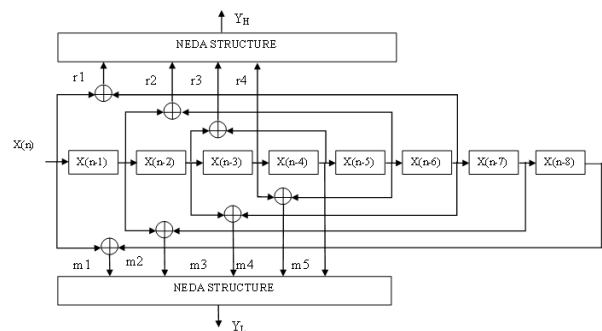
$$r(1)=X(n)+X(n-6)$$

$$r(2)=X(n-1)+X(n-5)$$

$$r(3) = X(n-2) + X(n-4)$$

$$r(4)=X(n-3)$$

We have used NEDA in 9/7 filter to remove multipliers. We have to apply NEDA two times get the 1-D 9/7 filter high pass output Y_{H1} and low pass output Y_{L1} .



Where h_0, h_1, h_2, h_3, h_4 are the Low pass filter coefficients and g_0, g_1, g_2, g_3 are the High pass filter coefficients.

If we take the high pass coefficients g_0, g_1, g_2 and g_3 applied NEDA technique by r_1, r_2, r_3 and r_4

then we get the high pass output Y_H of the 9/7 filter and we take the low pass coefficient h_0, h_1, h_2, h_3 , and h_4 applied NEDA technique by m_1, m_2, m_3, m_4 and m_5 then we get the low pass output Y_L of the 9/7 filter. Example the low pass output step by step as shown in below:

$$Y_L = [h_0 \ h_1 \ h_2 \ h_3 \ h_4] \cdot \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ m_5 \end{bmatrix}$$

Let $m_1 = 1$, $m_2 = 2$, $m_3 = 3$, $m_4 = 4$ and $m_5 = 5$. Then multiplier row and column and find out the low pass output 122. Where h_0, h_1, h_2, h_3 , and h_4 daubechies 9/7 filter coefficients are 0.6029490, 0.2668444, -0.782232, -0.0168641 and 0.02674875 respectively. All the daubechies 9/7 filter coefficients multiplied by 128 and get the 77, 34, -10, -2 and 3 respectively.

$$Y_H = [77 \ 34 \ -10 \ -2 \ 3] \cdot \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix} = 122$$

We take the low pass coefficients h_0, h_1, h_2, h_3 , and h_4 applied NEDA technique by m_1, m_2, m_3, m_4 and m_5 then we get the low pass output Y_L of the 9/7 filter.

$$Y_L = [01001101 \ 00100010 \ 11110110 \ 11111110 \ 0000001] \times \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ m_5 \end{bmatrix}$$

Now we can make the DA matrix by the filter coefficients as low pass filter based DA matrix

$$[X_k] = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 \end{bmatrix}$$

$$[Y_k] = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ m_5 \end{bmatrix} = \begin{bmatrix} m_1+m_5 \\ m_2+m_3+m_4+m_5 \\ m_1+m_3+m_4 \\ m_1+m_4 \\ m_3+m_4 \\ m_2+m_3+m_4 \\ m_1+m_3+m_4 \\ m_3+m_4 \end{bmatrix}$$

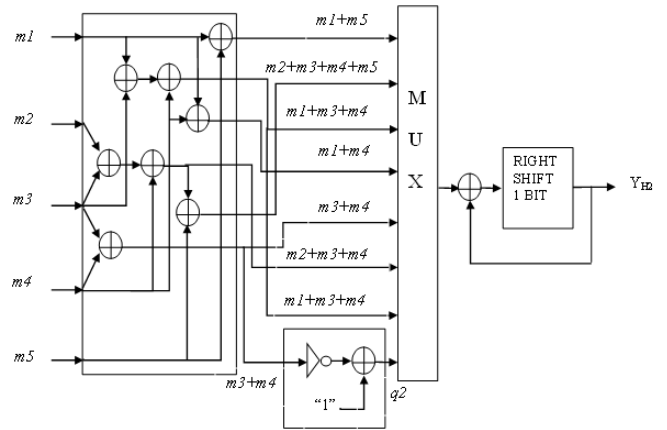


Figure 2: Proposed Architecture 1-D for Low Pass Filter Using NEDA Technique

IN Figure 3.9, apply NEDA techniques step-1 all the input converts' binary number

$$m_1 = 001, m_2 = 010, m_3 = 011, m_4 = 100, m_5 = 101$$

Step-2 all the binary input applied to sign extension so,

$$s(1) = 0001, s(2) = 0010, s(3) = 0011, s(4) = 0100, s(5) = 0101$$

Step-3 all the sign extension input applied to adder array so,

$$m(1) = 0110, m(2) = 1110, m(3) = 1000, m(4) = 0101, m(5) = 0111, m(6) = 1001, m(7) = 1000$$

$$m(8) = \text{not}(m_3 + m_4) + 1 = 1001$$

Step-4 the entire adder array input applied to MUX so,

The entire adder array input $m(1)$ right shift 1-bit so

$$\text{MUX}(1) = 0^*0110 = Y_p(0)$$

MUX (1) add MUX (2) = $Y_p(1)$

$$= 0'0110$$

$$= 1110$$

$$+ 100010$$

Output of the $Y_p(1)$ again right shift 1-bit and adds

MUX (3) so

$$= 0'100010$$

$$= 1000$$

$$+ 1100010$$

Continuous the process one by one, after then calculate the final output

$$Y_p(7) = 00001111010 = 122$$

Carry is rejected.

For 2-D sub-band WT, the outputs of 1-D high pass and low pass filters Y_{H1} and Y_{L1} are passed through series of shift registers and then we take the samples parallel using parallel data access method. The parallel data access method is used to minimize the memory requirement in 2-D sub-band WT.

IV. SIMULATION RESULT

All the designing and experiment regarding algorithm that we have mentioned in this paper is being developed on Xilinx 14.1i updated version. Xilinx 14.1i has couple of the striking features such as low memory requirement, fast debugging, and low cost. The latest release of ISE™ (Integrated Software Environment) design tool provides the low memory requirement approximate 27 percentage low. ISE 14.1i that provides advanced tools like smart compile technology with better usage of their computing hardware provides faster timing closure and higher quality of results for a better time to designing solution. By the aid of that software we debug the program easily. Also included is the newest release of the chip scope Pro Serial IO Tool kit, providing simplified debugging of high-speed serial IO designs for Virtex-7 FX and Virtex-6 LXT and SXT FPGAs. With the help of this tool we can develop in the area of communication as well as in the area of signal processing and VLSI low power designing. We functionally 2-D sub-band WT verified presented in this paper including all low pass filter and high pass filter. We have been found from the results shown in table 1, that number of slices, number of slices LUTs and maximum combinational path delay used in different types of device family. RTL (resister transistor logic) view is 2-D sub-band tree structure in shown in figure 3.

Table 1: Comparisons Result for 2-D Sub-band WT using Different types of Device Family

Device Family	2-D Sub-band Wavelet Transform		
	Number of Slice	Number of Slice LUTs	Maximum Combinational Path Delay
Vertex 7	233	975	17.411
Vertex 6	232	971	18.612
Spartan 6	236	975	42.527
Spartan 3	697	224	51.837

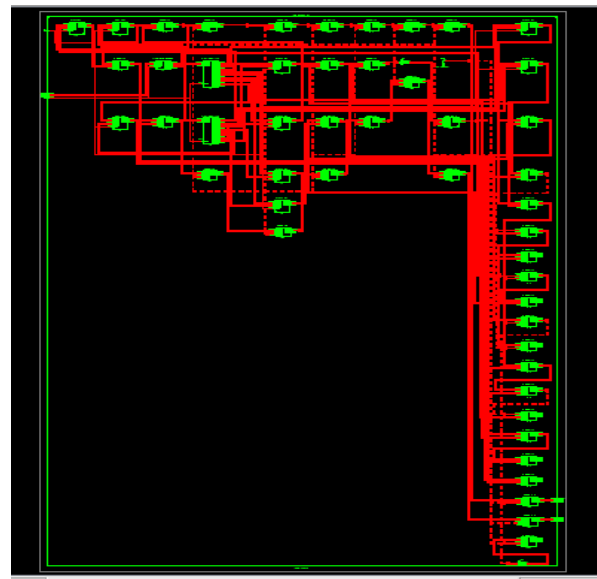


Figure 3: RTL View of 2-D Sub-band Wavelet Transform

2-D sub-band wavelet transform standardize two basic blocks for representing the image compression namely, low pass filter and high pass filter. Wavelet transforms a vast application in many areas like image compression, signal processing and VLSI design. We propose a 2-D sub-band novel distributed arithmetic paradigm named NEDA structure for VLSI implementation of digital signal processing (DSP) algorithms involving inner product of vectors and vector-matrix multiplication. We demonstrate that NEDA is a very efficient architecture with adders as the main component and free of ROM (free memory), multiplication, and subtraction. For the adder array, a systematic approach is introduced to remove the potential redundancy so that minimum additions are necessary.

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